

# A Model for Vague Association Rule Mining in Temporal Databases

Anjana Pandey<sup>1</sup>, K.R.Pardasani<sup>2</sup>

<sup>1</sup> Deptt of Information Technology, University Institute of Technology, RGPV, Bhopal, India

<sup>2</sup> Deptt of Mathematics, Maulana Azad National Institute of Technology, Bhopal, India

(Received October 15, 2012, accepted December 29, 2012)

**Abstract.** There are different university offering different types of courses over several years, and the biggest issue with that is how to get information to make course more effective. In real life these types of database usually contain temporal coherences, which cannot be captured by means of standard association rule mining. Here temporal Association rule mining can be used to evaluate the course effectiveness and helps to look for in regards to changes in performance of the course from time to time. For Example there is a course offering different topics. We can say that the topics having full attendance are totally effective and carry no hesitation information. While there are some topics which are almost fully attendant carry some hesitation information. This hesitation information is valuable and can be used to make the course more effective and interesting. Thus there is need for developing temporal vague association rule algorithms that reveal such hesitation information and temporal coherences within this data.

**Keywords:** *Hesitation Information, Vague Association Rule, AH pair, Temporal database.*

## 1. Introduction

The problem of the discovery of association rules comes from the need to discover patterns in transaction data in a supermarket. But transaction data are temporal. For example, when gathering data about products purchased in a supermarket, the time of the purchase is registered in the transaction. This is called *transaction time*, in temporal databases jargon, which matches the *valid time*, corresponding to the time of the business transaction confirmation at the register [1]. In large data volumes, as used for data mining purposes, we may find information related to products that did not necessarily exist throughout the data gathering period. So we can find some products that, at the moment of performing that mining, have already been discontinued. There may be also new products that were introduced after the beginning of the gathering. Some of these new products should participate in the associations, but may not be included in any rule because of support restrictions. For example, if the total number of transactions is 30,000,000 and we fix as minimum support 0.5 %, then a particular product must appear in, at least, 150,000 transactions to be considered frequent. Moreover, suppose that these transactions were recorded during the last 30 months, at 1,000,000 per month. Now, take a product that has been sold during the 30 months and has just the minimum support: it appears on average in 5,000 transactions per month. Consider now another product that was incorporated in the last 6 months and that appears in 20,000 transactions per month. The total number of transactions in which it occurs is 120,000; for that reason, it is not frequent, even though it is four times as popular as the first. However, if we consider just the transactions generated since the product appeared in the market, its support might be above the stipulated minimum. In this example, the support for the new product would be 2%, relative to its lifetime, since in 6 months the total of transactions would be about 6,000,000 and this product appears in 120,000 of them. Therefore, these new products would appear in interesting and potentially useful association rules. Each item, itemsets and rule has now an associated lifespan [2] which comes from the explicitly defined time in database transactions. The concept of temporal support is employed to mine association rules.

There are many items that are not bought but customers may have considered buying them. We call such information on a customer's consideration to buy an item the hesitation information [3] of the item,

since the customer hesitates to buy it. The hesitation information of an item is useful knowledge for boosting the sales of the item within given time period.

However, such information has not been considered in traditional association rule mining due to the difficulty to collect the relevant data in the past. Nevertheless, with the advances in technology of data dissemination, it is now much easier for such data collection.

A typical example is an online shopping scenario, such as “Amazon.com”, for which it is possible to collect huge amount of data from the Web log that can be modeled to mine hesitation information. From Web logs, we can infer a customer’s browsing pattern in a trail, say how many times and how much time s/he spends on a Web page, at which steps s/he quits the browsing, what and how many items are put in the basket when a trail ends, and so on. Therefore, we can further identify and Categorize different browsing patterns into different hesitation information with respect to different applications. The hesitation information can then be used to design and implement selling strategies that can potentially turn those “interesting” items into “under consideration” items and “under consideration” items into “sold” items.

From the literature [4], it is evident that very little attention has been paid for mining hesitation information. In this paper an attempt has been made to develop a vague set model for mining hesitation information within given time period. It is illustrated with the help of problem of choosing a course in an educational institute.

There are many different type of status of a piece of hesitation information (called hesitation status (HS)) [5]. Let us consider an example of class scenario that involves following type of status: (s1) attended class between 0 - 20%; (s2) Attended class between 0-40% (s3) Attended class between 0-60%. All of the above-mentioned types of HS are the hesitation information of those classes. Some of the types of HS are comparable based on some criterion, which means we can define an order on these types of HSs. For example, given a criterion as the possibility that the student attended the classes, we have  $S_1 \leq S_2 \leq S_3$ .

Here we are employ the vague set theory [3,4,5] to model the hesitation status of the course attended by the students. The main benefit of this approach is that the theory addresses the drawback of a single membership value in fuzzy set theory [6] by using interval-based membership that captures three types of evidence with respect to an object in a universe of discourse: support, against and hesitation. Thus, we naturally model the hesitation information of a course in the mining context as the evidence of hesitation.

The information of the “attended the class” and the “not attended the class” (without any hesitation information) in the traditional setting of association rule mining correspond to the evidence of support and against with respect to the class.

To study the relationship between the support evidence and the hesitation evidence with respect to topics, the concepts of attractiveness and hesitation are used, which are derived from the vague membership in vague sets. A topic with high attractiveness means that the topic is well attended and has a high possibility to be attended again next time. A topic with high hesitation means that the student is always hesitating to attend the topic due to some reason but has a high possibility to attend it next time if the reason is identified and resolved. For example, given the vague membership value, [0.5, 0.7], of a topic, the attractiveness is 0.6 (the median of 0.5 and 0.7) and the hesitation is 0.2 (the difference between 0.7 and 0.5), which implies that the student may attend the topic next time with a possibility of 60% and hesitate to attend the topic with a possibility of 20%. Using the attractiveness and hesitation of topics, we model a database with hesitation information as an AH-pair[4] database that consists of AH-pair transactions, where A stands for attractiveness and H stands for hesitation. Based on the AH-pair database, we then employed the notion of Vague Association Rules, which capture four types of relationships between two sets of items: the implication of the attractiveness/ hesitation of one set of items on the attractiveness/hesitation of the other set of items. For example, if we find an AH-rule like “People always buy quilts and pillows (A) but quit the process of buying beds at the step of choosing delivery method (H)”. Thus, there might be something wrong with the delivery method for beds (for example, no home delivery service provided) which causes people hesitate to buy beds. To evaluate the quality of the different types of Vague Association Rule, four types of support and confidence are defined. We also investigate the properties of the support and confidence of Vague Association Rule, which can be used to speed up the mining process. To show the incidence of time in the amount and quality of the obtained rules we extend, vague association rule algorithm that generates the frequent itemsets. Proposed Algorithm is based on the items’ period of life or lifespan.

This paper is organized as follows. Section 2 gives some preliminaries on vague set and temporal association rules. Section 3 discusses the algorithm that mines vague association rules. Section 4 illustrates the example. Section 5 reports the experimental results. Section 6 concludes the paper.

## 2. Preliminaries

The following definitions have been used to develop the model and algorithm for mining vague association rules.

### Definition 2.1 Vague Sets

Let  $I$  be a classical set of objects, called the universe of discourse, where an element of  $I$  is denoted by  $x$ .

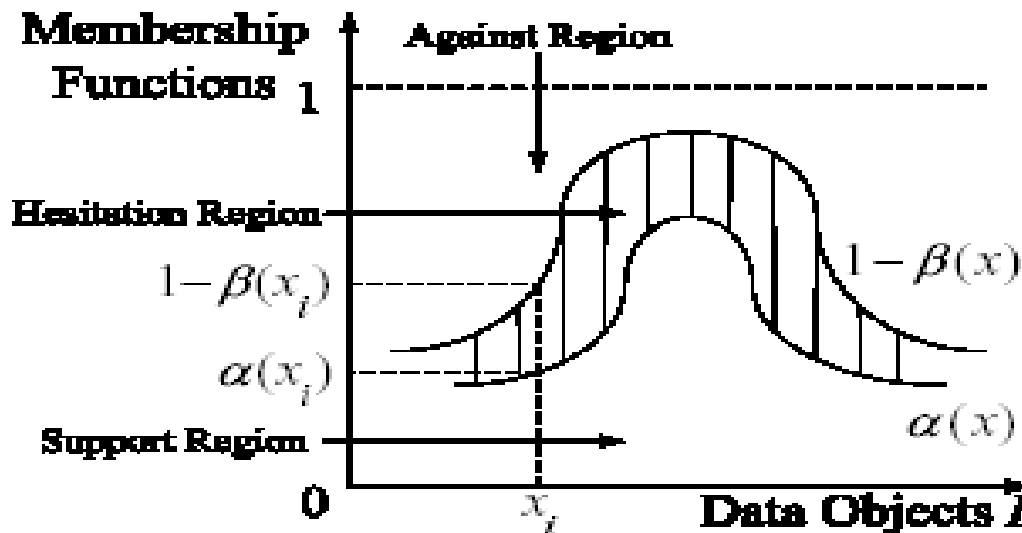


Figure 1 The true ( $\alpha$ ) and false ( $\beta$ ) Membership functions of a vague Set

A vague set  $V$  in a universe of discourse  $I$  is characterized by a true membership function,  $\alpha_v$ , and a false membership function,  $\beta_v$ , as follows:  $\alpha_v : I \rightarrow [0,1]$ ,  $\beta_v : I \rightarrow [0,1]$ , where  $\alpha_v(x) + \beta_v(x) \leq 1$ ,  $\alpha_v(x)$  is a lower bound on the grade of membership of  $x$  derived from the evidence for  $x$ , and  $\beta_v(x)$  is a lower bound on the grade of membership of the negation of  $x$  derived from the evidence against  $x$ . Suppose  $I = \{x_1, x_2, \dots, x_n\}$ . A vague set  $V$  of the universe of discourse  $I$  is represented  $V = \sum_{i=1}^n [\alpha(x_i), 1 - \beta(x_i)] / x_i$ , where  $0 \leq \alpha(x_i) \leq (1 - \beta(x_i)) \leq 1$ .

The grade of membership of  $x$  is bounded to  $[\alpha(x), 1 - \beta(x)]$ , which is subinterval of  $[0,1]$  fig (1). Here  $[\alpha(x), 1 - \beta(x)] / x$  is a vague element and the interval  $[\alpha(x), 1 - \beta(x)]$  is the vague value of the object  $x$ . For example,  $[\alpha(x), 1 - \beta(x)] = [0.5, 0.7]$  is interpreted as “the degree that the object  $x$  belongs to the vague set  $V$  is 0.5 (i.e.  $\alpha(x)$ ) and the degree that  $x$  does not belong to  $V$  is 0.3 (i.e.  $\beta(x)$ ).” For instance, in a voting process, the vague value  $[0.5, 0.7]$  can be interpreted as “50% of the votes support the motion, 30% are against, while 20% are neutral (abstentions).”[5]

### Definition 2.2 Median Memberships and Imprecision Memberships

To compare vague values, we use two derived memberships: median membership and imprecision membership [5]. We have unique median membership  $M_m(x)$  and imprecision membership  $M_i(x)$ , for a given vague value  $[\alpha(x), 1 - \beta(x)]$ .

Median membership is defined as  $M_m = \frac{1}{2}(\alpha + (1 - \beta))$ , which represents the overall evidence contained in a vague value. It can be checked that  $0 \leq M_m \leq 1$ . The vague value  $[1, 1]$  has the highest  $M_m$ , which means the corresponding object definitely belongs to the vague set (i.e., a crisp value). While the vague value  $[0, 0]$  has the lowest  $M_m$ , this means that the corresponding object definitely does not belong to the vague set.

Imprecision membership is defined as  $M_i = ((1 - \beta) - \alpha)$ , which represents the overall imprecision of a vague value. It can be checked that  $0 \leq M_i \leq 1$ . The vague value  $[a, a] (a \in [0, 1])$  has the lowest  $M_i$  which means that the membership of the corresponding object is exact (i.e., a fuzzy value). While the vague value  $[0, 1]$  has the highest  $M_i$  which means that we do not have any information about the membership of the corresponding object? The median membership and the imprecision membership are employed to measure the attractiveness and the hesitation of a topic with respect to a student.

A hesitation status (HS) is a specific state between two certain situations of “attending” (100% classes) and “not attending” (0 % classes) the class of the particular topic of a course. The hesitation information is formally defined as follows.

**Definition 2.3** (Hesitation and Overall Hesitation)

Given an item  $x \in I$  and a set of HS  $S = \{S_1, S_2, \dots, S_w\}$  with a partial order  $\leq$ . The hesitation of  $x$  with respect to an HS  $S_i \in S$  is a function  $h_i(x) : I \rightarrow [0, 1]$ , such that  $\alpha(x) + \beta(x) + \sum_{i=1}^w h_i(x) = 1$ , where

$h_i(x)$  represent the evidence for the HS  $S_i$  of  $x$ . The overall hesitation of  $x$  with respect to  $S$  is given by

$$H(x) = \sum_{i=1}^w h_i(x) [3].$$

**Definition 2.4** (Intent and Overall Intent)

Given a set of HS,  $(S, \leq)$ , the intent of an item  $x$  with respect to HS  $S_i \in S$ , denoted as  $\text{int}(x, S_i)$ , is a vague value  $[\alpha_i(x), 1 - \beta_i(x)]$  which is a subinterval of  $[\alpha(x), 1 - \beta(x)]$

and satisfy the following conditions

1.  $(1 - \beta_i(x)) = \alpha_i(x) + h_i(x)$
2. if  $S_i$  is in chain of the CG,  $S_1 \leq S_2 \leq \dots \leq S_i$ , then for  $1 \leq i \leq n$  we define

$$\alpha_i(x) = \frac{\alpha(x) + (1 - \beta(x))}{2} - \frac{1}{2} \sum_{k=1}^n h_k(x) + \sum_{k=1}^{i-1} h_k(x)$$

The overall intent of  $x$ , denoted as  $\text{INT}(x)$ , is the interval  $[\alpha(x), 1 - \beta(x)]$  [3].

**Definition 2.5** (Attractiveness and overall Attractiveness)

The attractiveness of  $x$  with respect to an HS  $S_i$ , denoted as  $\text{att}(x, S_i)$  is defined as the median membership of  $x$  with respect to  $S_i$ , that is  $\frac{1}{2}(\alpha_i(x) + (1 - \beta_i(x)))$ . The overall attractiveness of  $x$  is a

function  $\text{ATT}(x) : I \rightarrow [0, 1]$ , such that  $\text{ATT}(x) = \frac{1}{2}(\alpha(x) + (1 - \beta(x)))$  [7].

**Definition 2.6**(AH-pair Transaction and Database)

An AH-pair transaction  $T$  is a tuple  $\langle \nu_1, \nu_2, \dots, \nu_m \rangle$  on an itemsets  $I_T = \{x_1, x_2, \dots, x_m\}$  where  $I_T \subseteq I$  and  $\nu_j = \langle M_A(x_j), M_H(x_j) \rangle$  is an AH pair of the item  $x_j$  with respect to a given HS or the overall hesitation, for  $1 \leq j \leq m$ . An AH-pair database is a sequence of AH-pair transactions [7].

**Definition 2.7** (Vague Association Rule)

A Vague Association Rule (VAR)  $r = (X \Rightarrow Y)$ , is an association rule obtained from an AH-pair database. There are four types of support and confidence to evaluate the VARs as follows.

**Definition 2.8** (Support)

Given an AH- pair database,  $D$ , we define four types of support for an itemset  $Z$  or a VAR  $X \Rightarrow Y$ , where  $X \cup Y = Z$  as follows [8].

1. The  $A$  - support of  $Z$ , denoted as  $A\text{sup } p(Z)$ , is defined as  $\frac{\sum_{T \in D} \prod_{z \in Z} M_A(z)}{|D|}$ .
2. The  $H$  -support of  $Z$ , denoted as  $H\text{sup } p(Z)$ , is defined as  $\frac{\sum_{T \in D} \prod_{z \in Z} M_H(z)}{|D|}$ .
3. The  $AH$  -support of  $Z$ , denoted as  $AH\text{sup } p(Z)$ , is defined as  $\frac{\sum_{T \in D} \prod_{x \in X, y \in Y} M_A(x) M_H(y)}{|D|}$ .
4. The  $HA$  -support of  $Z$ , denoted as  $HA\text{sup } p(Z)$ , is defined as  $\frac{\sum_{T \in D} \prod_{x \in X, y \in Y} M_H(x) M_A(y)}{|D|}$ .

$Z$  is an  $A$  (or  $H$  or  $AH$  or  $HA$ ) FI if the  $A$  - or  $H$  or  $AH$  or  $HA$ ) support of  $Z$  is no less than the (respective  $A$  or  $H$  or  $AH$  or  $HA$ ) minimum support threshold where FI means frequent itemsets.

**Definition 2.9** (Confidence)

Given an AH- pair database,  $D$ , we define four types of support for an itemset  $Z$  or a VAR  $X \Rightarrow Y$ , where  $X \cup Y = Z$  as follows[8].

1. If both  $X$  and  $Y$  are  $A$  FIs, then the confidence of  $r$ , called the  $A$  -confidence of  $r$  and denoted as  $A\text{conf}(r)$ , is defined as  $\frac{A\text{sup } p(Z)}{A\text{sup } p(X)}$ .
2. If both  $X$  and  $Y$  are  $H$  FIs, then the confidence of  $r$ , called the  $H$  -confidence of  $r$  and denoted as  $H\text{conf}(r)$ , is defined as  $\frac{H\text{sup } p(Z)}{H\text{sup } p(X)}$ .
3. If  $X$  is an  $A$  FI and  $Y$  is an  $H$  FIs, then the confidence of  $r$ , called the  $AH$  confidence of  $r$  and denoted as  $AH\text{conf}(r)$ , is defined as  $\frac{AH\text{sup } p(Z)}{H\text{sup } p(X)}$ .
4. If  $X$  is an  $H$  FI and  $Y$  is an  $A$  FIs, then the confidence of  $r$ , called the  $HA$  confidence of  $r$  and denoted as  $HA\text{conf}(r)$ , is defined as  $\frac{HA\text{sup } p(Z)}{H\text{sup } p(X)}$ .

**Definition 2.10** (Temporal Support)

The *support* of  $X$  in  $d$  over its lifespan  $I_x$ , denoted  $S(X, I_x, d)$ , is the fraction of transactions in  $d$  that contains  $X$  during the interval of time corresponding to  $I_x$ :  $|V(X, d)| / |d_{IX}|$ . The *frequency* of a set  $X$  is its support. Given a threshold of support  $\sigma \in [0,1]$  and a threshold of temporal support  $\tau$ ,  $X$  is *frequent* in its lifespan  $I_x$  if  $S(X, I_x, d) \geq \sigma$  and  $|I_x| \geq \tau$ . Here  $X$  has *minimum support* in  $I_x$ .

The support threshold or frequency  $\sigma$  is a parameter given by the user and is dependent on the application. The temporal support threshold is given by the user [1].

**3. Genetic Algorithm**

Here we present an algorithm to mine Vague Association Rules from temporal database. We first mine the set of all  $A, H, AH$  and  $HA$  frequent itemset ( $FI$ ) from the input  $AH$  pair database with respect to certain  $HS$  or the overall hesitation. Then, we generate the Vague Association Rules from the set of FIs.

To generate the  $A, H, AH$  and  $HA$  pair from the database first module is developed to calculate the Intent of an item. The intent of an item  $x$ , denoted as  $\text{intent}(x)$ , is a vague value  $[\alpha(x), 1 - \beta(x)]$ . The vague value of intent is calculated using the Algorithm **CalIntent()**.

The  $\text{calIntent}()$  Algorithm which is first module is a nested iterative method to calculate the intent. This algorithm takes a Data-set ( $D$ ) as input as given in the Table 1. This Data-set consists of rows and column as student ID ( $S\_ID$ ) and topic ID ( $T\_ID$ ) of the course. Therefore, data set  $D$  is considered as a two dimensional array. Step 1 initializes the intent array (having size as no. of topics) while Step 2 and Step 4 are used to navigate in the Data-set array. In Step 3 favor ( $\alpha$ ) and against ( $\beta$ ) are initialized to store overall favor and against which is finally stored in the intent array in the Step 8. This algorithm returns an intent array as shown in Table 2.

**Algorithm CalIntent(D)**

1. Initialize intent array to store intent;
2. For each  $i=0,1,2,\dots$  where  $i < \text{no. of tpID}$ , do
3. Initialize favor( $\alpha$ ) & against( $\beta$ ) variable with value zero;
4. For each  $j=0,1,2,\dots$  where  $j < \text{no. of stID}$ , do
5. Increment favor( $\alpha$ ) by one when  $D[i][j]$  is equal to one;
6. Increment against( $\beta$ ) by one when  $D[i][j]$  is equal to zero;
7. End of for ;
8. Generate intent using favor and against as  $[\alpha, 1-\beta]$  ;
9. End of for;
10. return all intent;

The **CalAHPair** Algorithm which is the second module is a simple iterative method to calculate the  $AH$  pair. This algorithm takes a Intent as input as given by algorithm 3.1. Step 1 initialize the  $AH$  pair array having size as no. of tpID. Step 2 is used to traverse the intent array while Step 3, 4, 5 are used to calculate attractiveness and hesitation to finally calculate the  $AH$  pair. This algorithm returns  $AH$ -pair array as shown in Table 3.

**Algorithm CalAHPair(intent)**

1. Initialize AHPair array to store AH pair;
2. For each  $i=0,1,2,\dots$  where  $i < \text{no. of tpID}$
3. Attractiveness as a median membership i.e.  $\frac{1}{2}(\alpha+(1-\beta))$ ;
4. Hesitation as a difference of  $\alpha$  and  $1-\beta$  using intent;
5. End of for;
6. return all AHPair;

Now we have  $AH$  pair database  $D$  to generate vague association rules. Let  $A_i$  and  $H_i$  be the set of  $A$  frequent itemset(FIs) and  $H$  frequent itemsets containing  $i$  items, respectively. Let  $A_iH_j$  be the set of  $AH$  frequent itemsets containing  $i$  items with  $A$  values and  $j$  items with  $H$  values. Here  $A_iH_j$  is equivalent to  $H_jA_i$ . Let  $C_w$  be the set of candidate FIs, from which the set of FIs  $W$  is to be generated, where  $W$  is  $A_i, H_i$ , or  $A_iH_j$ .

In proposed Algorithm database  $D'$ , has lower limit ( $t_1$ ) and upper limit ( $t_2$ ) of the life time of the item, and counting the support of the itemset in the interval  $[t_1, t_2]$ .

Let  $A_i[t_1, t_2]$  and  $H_i[t_1, t_2]$  be the set of  $A$  frequent itemset and  $H$  frequent itemset containing  $i$  items, respectively. Let  $A_iH_j[t_1, t_2]$  be the set of  $AH$  FIs containing  $i$  items with  $A$  values and  $j$  items with  $H$  values. Let  $C_w[t_1, t_2]$  be the set of candidate FIs, from which the set of FIs  $W$  is to be generated, where  $W$  is  $A_i, H_i$ , or  $A_iH_j$ .

**Algorithm 5.4:MineVFI( $D', \sigma, \tau$ )**

$D'$ : Temporal database.

$\sigma$ :Support and  $\tau$ :Temporal Support

1. Initialize  $FIs$  array to store  $FI$
2. Mine  $A_1$  and  $H_1$  from  $D'$ : //for each itemset of size 1, and time of its first appearance in  $t_1$  and the time of its last appearance in  $t_2$
3. Calculate the temporal- support and support of  $A_1$  and  $H_1$  where temporal-Support  $> \tau$  and support  $> \sigma$ .
4. Generate  $C_{A_2}$  from  $A_1$ ,  $C_{A_1H_1}$  from  $A_1$  and  $H_1$ , and  $C_{H_2}$  from  $H_1$ ;
5. Calculate the temporal support and support of  $C_{A_2}$ ,  $C_{A_1H_1}$  and  $C_{H_2}$  to give  $A_2, A_1H_1$  and  $H_2$ , respectively;
6. for each  $k = 3, 4, \dots$ , where  $k = i + j$ , do
7. Generate  $C_{A_k}$  from  $A_{i-1}$  and  $C_{H_k}$  from  $H_{i-1}$ , for  $i = k$ ;
8. Generate  $C_{A_iH_j}$  from  $A_{i-1}H_j$ , for  $2 \leq i < k$  and from  $A_1H_{j-1}$ , for  $i = 1$ ;
9. Calculate the temporal support and support of  $C_{A_k}$ ,  $C_{A_iH_j}$  and  $C_{H_k}$  to give  $A_k, A_iH_j$  and  $H_k$ , respectively;
10. If all  $A, H, AH$ , are greater than  $\sigma$  and  $\tau$  add into the array *Frequent Itemset FIs*;
11. return all *Frequent Itemset FIs*

Table 1 shows the data of student, where 1 and 0 represents that student attended the class and student does not attended the class (without any hesitation information) with respect to given week. The set of hesitation status is given by  $S = \{S_1, S_2, S_3, S_4, S_5\}$ . The table 1 is constructed using data regarding attendance of course data structure taught in UIT RGPV Bhopal.

Table 1 Sample Database of Attendance

S_ID	T_ID=1	T_ID=2	T_ID=3	T_ID=4
1	1	s4	s4	s1
2	1	0	s1	0
3	1	1	s3	s3
4	0	s5	s2	s3
5	s1	1	s5	s2
6	1	0	s3	s5
7	1	s5	s4	0
8	s1	0	0	s2
9	s3	0	1	0
10	1	s5	0	s5
Time	1 week	2 week	3 week	4 week

Now  $X_I = \{\text{Topic 1}\}$ ,  $I_{X_I} = [1,4]$ , which have stamped times 1 and 4. Similarly for topic2,3,and 4 assign the time stamp.

Now we calculate the intent and AH pair with respect to s1.

**Calculating intent:**

Table 2 Intent of Topic with respect to s1

	T_ID=2	T_ID=3	T_ID=4
[0.6,0.9]	[0.2,0.6]	[0.1,0.8]	[0.0,0.7]

**Calculating AH pair:**

Table 3 AH –pair database with respect to S1

T_ID=1	T_ID=2	T_ID=3	T_ID=4
[0.750,0.29]	[0.40,0.40]	[0.45,0.70]	[0.35,0.70]

**Calculating support:**

Here support is calculated with given time stamp.

Table 4 four types of Support of  $C \Rightarrow A[1,3]$ 

A	H	AH	HA
[0.1125]	[0.0699]	[0.4496]	0.175]



Table 5 four types of Support of  $B \Rightarrow A[1,3]$ 

A	H	AH	HA
[0.15]	[0.0595]	[0.055]	[0.15]

Table 6 four types of Support of  $D \Rightarrow B[2,4]$ 

A	H	AH	HA
[0.07]	[0.09]	[0.0466]	[0.0933]

#### 4. PERMORFANCE EVALUTION AND EXPERIMENT

To present the scale-up properties of our algorithms, we performed experiments on a 2.4GHz, 512 Mb PC running Windows XP Professional. The algorithm is implemented in Java. For the experiment, the data of attendance of the Data-structure Course, taught in Information Technology of UIT-RGPV Bhopal is used to prepare the Data-set (D) according to the format illustrated in the table 1 as a array in which column contains the Hesitation status of different topics ( introduction to data structure, array, stacks, queue ..... ) and rows contains student IDs. The trends discovered are aggregated to finally make conclusion.

We identify many trails on the data-set and aggregated them to finally come to a conclusion.

When  $\sigma=0.002$  we obtain many vague association rules some of them are as given.

1.  $Array \Rightarrow Stack [1,3]$  With  $HA$  support =0.78.

Rule 1 shows that topic Array is prerequisite for topic Stack .Topic of Stack heavily depended on Array topic. If the students have no knowledge of Arrays then students show more hesitation to attend the lectures on Stacks.

2.  $Stack \Rightarrow Queue [1,4]$  With  $HA$  support = 0.10

Rule 2 illustrates that topic of Stack is not prerequisite for the topic Queue and there is little dependency among them. So students can directly attend the lecture of Queue with less hesitation.

3.  $Array, Tree \Rightarrow Graph [2,4]$  with  $HA$  support = 0.42

Rule 3 shows that the Introduction of Graph depended on the topic Array and queue both with the  $HA$  support 0.42 which finally concluded that when the topic Graph are taught without introduction of Array and Tree then student feels hesitation to attend that course .

Figure.2 and Figure. 3 report the running time and the number of FIs. From Figure 2 , the running time decreases with the Increase in the value of  $\sigma$  due to the larger number of *frequent Itemset (FIs)* generated. Figure 3, shows that the number of *frequent Itemset FIs* decrease with the support increases.

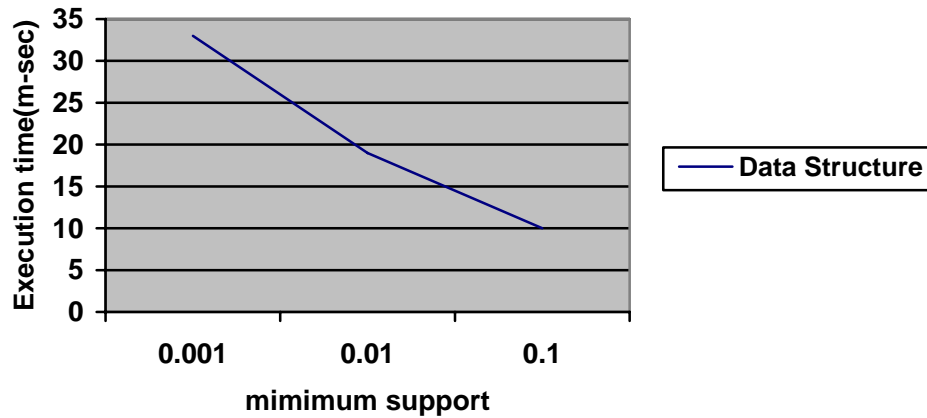


Fig.2 Running Time of Frequent itemset

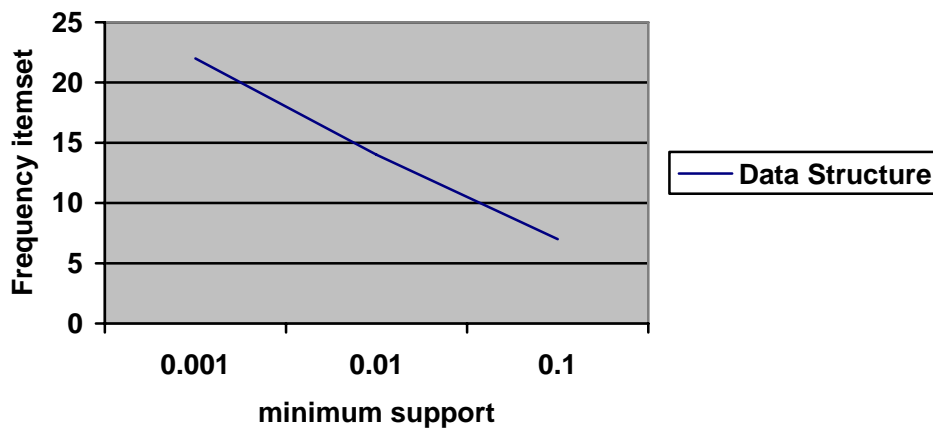


Fig.3 Number of Frequent Itemset

## 5. Conclusion

The models for hesitation information is developed by vague set theory in order to address a limitation in traditional association rule mining problem, which ignores the hesitation information of items in transactions. The efficient algorithm for mining vague association rule that discovers the hesitation information of items is proposed in one paper (which is the process of publication). Also this algorithm is extended for mining temporal association rule. The effectiveness of algorithm is also revealed by experiments on real datasets. This algorithm has wide applications for example different ranking scores together with click through data of a search result can be modeled as an object having different hesitation status. In this case vague association rule can be used to reflect different users' preferences. Such models can further be developed and extended to problems involving mining of hesitation information in different conditions.

## 6. References

- [1] Agrawal.R and Srikant.R. Fast algorithms for mining association rules. In Proc. of the 20th Int'l Conference on Very Large Databases,1994 Santiago, Chile.
- [2] An Lu and Wilfred Ng "Maintaining consistency of vague databases using data dependencies"Data and Knowledge Engineering,Volume 68,2009,Pages 622-641.

- [3] Lu, A., Ng, W. "Managing merged data by vague functional dependencies". In: Atzeni, P., Chu, W., Lu, H., Zhou, S., Ling, T.-W. (eds.) ER 2004. LNCS, vol. 3288, pp. 259–272. Springer, Heidelberg.
- [4] An Lu and Wilfred Ng "Mining Hesitation Information by Vague Association Rules" *Lecture Notes in Computer Science*, Springer Volume 4801/, 2008, pg 39-55.
- [5] Gau, W.-L., Buehrer, D.J. "Vague sets". *IEEE Transactions on Systems, Man, and Cybernetics* 23(2), 1993, 610–614 .
- [6] Lu, A., Ng, W. "Vague sets or intuitionistic fuzzy sets for handling vague data": Which one is better? In: Delcambre, L.M.L., Kop, C., Mayr, H.C., Mylopoulos, J., Pastor, O. (eds.) ER 2005. LNCS, vol. 3716, pp. 401–416. Springer, Heidelberg.
- [7] Zadeh L. A., "Fuzzy sets," *Inform. Contr.*, vol. 8, 1965, pp. 338–353.
- [8] Lu, A., Ng, W.: Handling Inconsistency of vague relations with functional dependencies. In :ER(2007). LNCS Vol 4321 pp 301-312.

